

# Electronic polarizability and crystallization of $K_2O$ – $TiO_2$ – $GeO_2$ glasses with high $TiO_2$ contents

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## Abstract

Some  $K_2O$ – $TiO_2$ – $GeO_2$  glasses with a large amount of  $TiO_2$  contents (15–25 mol%) such as  $25K_2O$ – $25TiO_2$ – $50GeO_2$  have been prepared, and their electronic polarizability, Raman scattering spectra, and crystallization behavior are examined to clarify thermal properties and structure of the glasses and to develop new nonlinear optical crystallized glasses. It is proposed that the glasses consist of the network of  $TiO_6$  and  $GeO_4$  polyhedra. The glasses show large optical basicities of  $A = 0.88$ – $0.92$ , indicating the high polarizability of  $TiO_n$  ( $n = 4$ – $6$ ) polyhedra in the glasses.  $K_2TiGe_3O_9$  crystals are formed through crystallization in all glasses prepared in the present study. In particular,  $20K_2O$ – $20TiO_2$ – $60GeO_2$  glass shows bulk crystallization and  $18K_2O$ – $18TiO_2$ – $64GeO_2$  glass exhibits surface crystallization giving the  $c$ -axis orientation. The crystallized glasses show second harmonic generations (SHGs), and it is suggested that the distortion of  $TiO_6$  octahedra in  $K_2TiGe_3O_9$  crystals induces SHGs.

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## 1. Introduction

In the area of photonics, transparent crystallized glasses consisting of nonlinear optical/ferroelectric crystals have received much attention, because such materials have a high potential for applications in laser hosts, tunable waveguides, tunable fiber gratings, and so on. In nonlinear optical crystals reported so far, there are many attractive  $TiO_2$ -based or-containing crystals, e.g.,  $BaTiO_3$  and  $KTiOPO_4$ . Adair et al. [1] demonstrated that  $TiO_2$  shows the highest nonlinear refractive index in a large number of optical crystals, indicating a very high oxygen hyperpolarizability of  $Ti$ – $O$  pairs. Dimitrov and Komatsu [2] indicated that  $TiO_2$ -based glasses have large oxide ion electronic polarizabilities. It is, therefore, of interest to fabricate glasses with a large amount of  $TiO_2$  and to synthesize  $TiO_2$ -based nonlinear optical crystals through crystallization of such glasses. Indeed, there has been some

reports on crystallized glasses consisting of nonlinear optical  $TiO_2$ -based crystals [3–16]. For instance, very recently, Kosaka et al. [7] demonstrated that crystallized glasses with  $Ba_3Ti_3O_6(BO_3)_2$  crystals show a strong second harmonic intensity.

It is also noted that there has been some reports on the crystallized glasses consisting of  $GeO_2$ -based or-containing nonlinear optical crystals such as  $LaBGeO_5$  and  $Bi_2GeO_5$  [16–28]. In Table 1, some studies on the synthesis of  $TiO_2$ -based or  $GeO_2$ -based crystals in the crystallization processing of glasses reported so far are summarized [3–28]. Among them, it should be pointed out that transparent crystallized glasses with ferroelectric  $Ba_2TiGe_2O_8$  crystals in the  $BaO$ – $TiO_2$ – $GeO_2$  system show a large second-order optical nonlinearity of  $d_{33} = \sim 20$  pm/V, being comparable to the values of  $LiNbO_3$  single crystal, as reported by Takahashi et al. [15,16].

In this study, we focus our attention on  $K_2O$ – $TiO_2$ – $GeO_2$  glasses containing both  $TiO_2$  and  $GeO_2$ . It is known that the  $K_2O$ – $TiO_2$ – $GeO_2$  system has a wide glass-forming region [29], meaning the possibility of the fabrication of

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glasses with a large amount of  $\text{TiO}_2$ . Since all oxides of  $\text{K}_2\text{O}$ ,  $\text{TiO}_2$ , and  $\text{GeO}_2$  have large oxide ion electronic polarizabilities [2,30,31], it is expected that  $\text{K}_2\text{O}$ – $\text{TiO}_2$ – $\text{GeO}_2$  glasses would indicate high refractive indices and might have a possibility of the formation of optical nonlinear crystals through crystallization. Very recently, Grujic et al. [32] have reported some thermal properties and crystallization behavior of  $20\text{K}_2\text{O}$ – $20\text{TiO}_2$ – $60\text{GeO}_2$  glass, but their information is limited. That is, there has been no report on physical properties such as refractive index, Raman scattering spectra, and nonlinear optical properties of crystallized samples for  $\text{K}_2\text{O}$ – $\text{TiO}_2$ – $\text{GeO}_2$  glasses. The purpose of this study is to search new nonlinear optical crystallized glasses showing second harmonic generation (SHG) through investigation of the crystallization behavior of some  $\text{K}_2\text{O}$ – $\text{TiO}_2$ – $\text{GeO}_2$  glasses with high  $\text{TiO}_2$  contents. At the same time, the electronic polarizability of the ions and the established features in the Raman spectra and crystallized products are used to clarify the structure and nonlinear optical properties of the materials.

Table 1  
 $\text{TiO}_2$ - or  $\text{GeO}_2$ -based glass systems and crystalline phases formed through crystallization reported so far

Glass system	Crystalline phase	Ref.
$\text{BaO}$ – $\text{TiO}_2$ – $\text{SiO}_2$ (or $\text{TeO}_2$ )	$\text{BaTiO}_3$	[3,4]
$\text{PbO}$ – $\text{TiO}_2$ – $\text{Al}_2\text{O}_3$ – $\text{SiO}_2$	$\text{PbTiO}_3$	[5]
$\text{BaO}$ – $\text{TiO}_2$ – $\text{B}_2\text{O}_3$	$\text{BaTi}(\text{BO}_3)_2$ , $\text{Ba}_3\text{Ti}_3\text{O}_6$ ( $\text{BO}_3$ ) <sub>2</sub>	[6–8]
$\text{BaO}$ – $\text{TiO}_2$ – $\text{SiO}_2$	$\text{Ba}_2\text{TiSi}_2\text{O}_8$	[9,10]
$\text{Bi}_2\text{O}_3$ – $\text{TiO}_2$ – $\text{Nb}_2\text{O}_5$ – $\text{B}_2\text{O}_3$ – $\text{SiO}_2$	$\text{Bi}_3\text{TiNbO}_9$	[11]
$\text{Bi}_2\text{O}_3$ – $\text{TiO}_2$ – $\text{B}_2\text{O}_3$	$\text{Bi}_4\text{Ti}_3\text{O}_{12}$	[12]
$\text{K}_2\text{O}$ – $\text{TiO}_2$ – $\text{P}_2\text{O}_5$ – $\text{SiO}_2$	$\text{KTiOPO}_4$	[13]
$\text{PbO}$ – $\text{GeO}_2$	$\text{Pb}_5\text{Ge}_3\text{O}_{11}$	[17,18]
$\text{La}_2\text{O}_3$ – $\text{B}_2\text{O}_3$ – $\text{GeO}_2$	$\text{LaBGeO}_5$	[19–22]
$\text{Li}_2\text{O}$ – $\text{B}_2\text{O}_3$ – $\text{GeO}_2$	$\text{LiBGeO}_4$	[23]
$\text{Bi}_2\text{O}_3$ – $\text{GeO}_2$ – $\text{B}_2\text{O}_3$	$\text{Bi}_2\text{GeO}_5$	[24]
$\text{K}_2\text{O}$ – $\text{Nb}_2\text{O}_5$ – $\text{GeO}_2$	$\text{K}_{3,8}\text{Nb}_5\text{Ge}_3\text{O}_{20,4}$	[25,26]
$\text{BaO}$ – $\text{Ga}_2\text{O}_3$ – $\text{GeO}_2$	$\text{Ba}_3\text{Ga}_2\text{Ge}_4\text{O}_{14}$	[27,28]
$\text{BaO}$ – $\text{TiO}_2$ – $\text{GeO}_2$	$\text{Ba}_2\text{TiGe}_2\text{O}_8$	[14–16]
$\text{K}_2\text{O}$ – $\text{TiO}_2$ – $\text{GeO}_2$	$\text{K}_2\text{TiGe}_3\text{O}_9$	[32]
		Present study

Table 2  
 Chemical compositions, glass transition,  $T_g$ , crystallization onset,  $T_x$ , and crystallization peak,  $T_p$ , temperatures, density  $d$ , and refractive index  $n$  of  $\text{K}_2\text{O}$ – $\text{TiO}_2$ – $\text{GeO}_2$  glasses

Glass composition (mol%)				$T_g$ (°C)	$T_x$ (°C)	$T_p$ (°C)	$d$ (g/cm <sup>3</sup> )	$n$
Sample	$\text{K}_2\text{O}$	$\text{TiO}_2$	$\text{GeO}_2$	±2	±2	±2	±0.002	±0.002
50KTG	25	25	50	515	596	612	3.344	1.705
60KTG	20	20	60	551	616	631	3.501	1.711
64KTG	18	18	64	554	636	651	3.574	1.716
60KTG-2	25	15	60	494	594	605	3.393	1.666
60KTG-3	15	25	60	559			3.591	1.766

## 2. Experimental

The chemical compositions of  $\text{K}_2\text{O}$ – $\text{TiO}_2$ – $\text{GeO}_2$  glasses prepared in the present study are given in Table 2. Glasses were prepared by using a conventional melt-quenching method. Commercial powders of reagent grade  $\text{K}_2\text{CO}_3$ ,  $\text{TiO}_2$ , and  $\text{GeO}_2$  were mixed together and melted in a platinum crucible at 1250 °C for 1 h in an electric furnace. The melts were poured onto an iron plate and pressed to a thickness of 1–1.5 mm by another iron plate. Glass transition,  $T_g$ , crystallization onset,  $T_x$ , and crystallization peak,  $T_p$ , temperatures were determined using differential thermal analyses (DTA) at a heating rate of 10 K/min. Densities of glasses were determined with the Archimedes method using distilled water as an immersion liquid. Refractive indices at a wavelength of 632.8 nm (He–Ne laser) were measured at room temperature with a prism coupler (Metricon Model 2010).

The glasses were heat treated at various temperatures, and the crystalline phases present in the heat-treated samples were examined by X-ray diffraction (XRD) analysis at room temperature using  $\text{Cu K}\alpha$  radiation and from Raman scattering spectra (Tokyo Instruments Co., Nanofinder operated at  $\text{Ar}^+$  (488 nm) laser). Second harmonic generations (SHGs) of crystallized samples were examined by Maker fringe techniques [33]. A fundamental wavelength of a Q-switched  $\text{Nd}^{3+}$ : yttrium-aluminum-garnet (YAG) laser operating at  $\lambda = 1064$  nm was used as the incident light, and the intensities of green light ( $\lambda = 532$  nm) emissions were measured. As polarization for second harmonic (SH) intensity measurements, the combination of  $p$ -excitation and  $p$ -detection ( $pp$ -polarization) was used.

## 3. Results

### 3.1. Thermal properties of glasses

In this study, five different glasses such as  $25\text{K}_2\text{O}$ – $25\text{TiO}_2$ – $50\text{GeO}_2$  (designated here as 50KTG glass),  $20\text{K}_2\text{O}$ – $20\text{TiO}_2$ – $60\text{GeO}_2$  (60KTG), and  $18\text{K}_2\text{O}$ – $18\text{TiO}_2$ – $64\text{GeO}_2$  (64KTG) were prepared, as shown in Table 2. Optically transparent bulk glasses were obtained for all compositions. DTA curves for some glasses are shown in

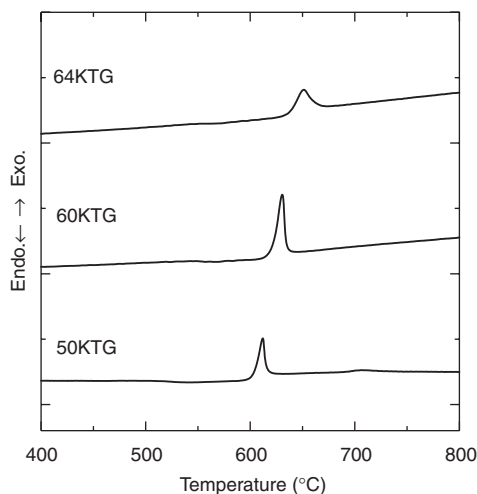


Fig. 1. DTA patterns for 50KTG, 60KTG, and 64KTG glasses. Heating rate was 10 K/min. 50KTG:  $25\text{K}_2\text{O}-25\text{TiO}_2-50\text{GeO}_2$ , 60KTG:  $20\text{K}_2\text{O}-20\text{TiO}_2-60\text{GeO}_2$ , 64KTG:  $18\text{K}_2\text{O}-18\text{TiO}_2-64\text{GeO}_2$ .

Fig. 1. It is seen that 60KTG glass shows a sharp crystallization peak. Contrary, in 64KTG glass, a broad crystallization peak is observed. These DTA data suggest that the crystallization behavior of  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses is sensitive to the glass composition. The values of  $T_g$ ,  $T_x$ , and  $T_p$  are summarized in Table 2, giving the values of  $T_g = 494-559^\circ\text{C}$ ,  $T_x = 594-636^\circ\text{C}$ , and  $T_p = 605-651^\circ\text{C}$ . In  $x\text{K}_2\text{O}-x\text{TiO}_2-(100-2x)\text{GeO}_2$  glasses, all values of  $T_g$ ,  $T_x$ , and  $T_p$  increase with increasing  $\text{GeO}_2$  content. In  $x\text{K}_2\text{O}-(40-x)\text{TiO}_2-60\text{GeO}_2$  glasses, the values of  $T_g$ ,  $T_x$ , and  $T_p$  increase with increasing  $\text{TiO}_2$  content. Considering that generally  $\text{K}_2\text{O}$ ,  $\text{TiO}_2$  and  $\text{GeO}_2$  in oxide glasses act as a network modifier, intermediate and network former, respectively, the composition dependence on these thermal properties ( $T_g$  and  $T_x$ ) in  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses would be reasonable.

The values of density,  $d$ , and refractive index,  $n$ , are given in Table 2. It is seen that both values in  $x\text{K}_2\text{O}-x\text{TiO}_2-(100-2x)\text{GeO}_2$  glasses increase with increasing  $\text{GeO}_2$  content.  $\text{TiO}_2$  in  $x\text{K}_2\text{O}-(40-x)\text{TiO}_2-60\text{GeO}_2$  glasses increases largely both density and refractive index. 60KTG glass, i.e.,  $20\text{K}_2\text{O}-20\text{TiO}_2-60\text{GeO}_2$  glass, for example, has the values of  $d = 3.501\text{ g/cm}^3$  and  $n = 1.711$ .

### 3.2. Electronic polarizability of glasses

One of the most important properties of materials, which is closely related to their applicability in the field of optics and electronics, is the electronic polarizability. Estimation of the state of polarizability of the ions is the subject of the so-called polarizability approach based on the Lorentz–Lorenz equation (Eq. (1)) giving the relationship between molar refraction,  $R_m$ , and refractive index,  $n$ :

$$R_m = \left[ \frac{(n^2 - 1)}{(n^2 + 2)} \right] \left( \frac{M}{d} \right) = \left[ \frac{(n^2 - 1)}{(n^2 + 2)} \right] V_m = \frac{4\pi\alpha_m N}{3}, \quad (1)$$

where  $M$  is the molecular weight,  $V_m$  is the molar volume,  $\alpha_m$  the molar polarizability, and  $N$  the Avogadro's number. Eq. (1) gives the average molar refraction for isotropic substances such as liquids, glasses and cubic crystals. The Lorentz–Lorenz equation allows calculating the so-called the electronic polarizability of oxide ions,  $\alpha_{\text{O}_2^-}(n)$  in oxide materials by subtracting the cation polarizability from the molar polarizability  $\alpha_m$ , taking into account the relationship proposed by Dimitrov and Sakka [30] for simple oxides and successfully applied for various oxide glasses [34,35]:

$$\alpha_{\text{O}_2^-}(n) = \left[ \frac{R_m}{2.52} - \sum \alpha_i \right] (N_{\text{O}_2^-})^{-1} \quad (2)$$

where  $\sum \alpha_i$  denotes molar cation polarizability and  $N_{\text{O}_2^-}$  denotes the number of oxide ions in the chemical formula. Furthermore, as discussed by Duffy [36], an intrinsic relationship exists between electronic polarizability of the oxide ions and so-called optical basicity of the oxide medium,  $A$ , as given by Eq. (3):

$$A = 1.67 \left( 1 - \frac{1}{\alpha_{\text{O}_2^-}} \right). \quad (3)$$

This relation presents a general trend toward an increase in the oxide ion polarizability with increasing optical basicity. The optical basicity of an oxide medium as proposed by Duffy and Ingram [37,38] is a numerical expression of the average electron donor power of the oxide species constituting the medium, and thus it is used as a measure of the acid–base properties of oxides, glasses, alloys, slags, molten salts, etc. Since increased oxide ion polarizability means stronger electron donor ability of oxide ions, the physical background of the oxide ion polarizability and optical basicity is naturally the same.

Using Eqs. (1), (2), and (3), we estimated the values of  $\alpha_m$ ,  $\alpha_{\text{O}_2^-}$  and  $A$  of  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses prepared in the present study, and the results are shown in Table 3. The data of the cation polarizability of  $\text{K}^+$ ,  $\text{Ti}^{4+}$  and  $\text{Ge}^{4+}$  are taken from Ref. [31]. As seen in Table 3, the glasses show the electronic polarizabilities of  $\alpha_{\text{O}_2^-} = 2.129 - 2.225 \text{ \AA}^3$  and the optical basicities of  $A = 0.886 - 0.919$ , indicating by this manner that the glasses investigated in this study are basic in nature. In  $x\text{K}_2\text{O}-x\text{TiO}_2-(100-2x)\text{GeO}_2$  glasses, the values of  $\alpha_m$ ,  $\alpha_{\text{O}_2^-}$  and  $A$  decrease with increasing  $\text{GeO}_2$  content. On the other hand, in  $x\text{K}_2\text{O}-(40-x)\text{TiO}_2-60\text{GeO}_2$  glasses, these values increase with increasing  $\text{TiO}_2$  content. It is, therefore, considered that  $\text{TiO}_2$  enhances the electronic polarizability in  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses. The relatively large values of  $\alpha_m$ ,  $\alpha_{\text{O}_2^-}$  and  $A$  obtained in the present study suggest that  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses have a high potential as nonlinear optical materials. The obtained values of the optical basicity of  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses are close to those of other  $\text{TiO}_2$ -based glasses such as  $\text{K}_2\text{O}-\text{TiO}_2$  and  $\text{PbO}-\text{TiO}_2$  for which have been reported values of  $A = 0.85 - 1.17$  [34]. Similarly, Kosaka et al. [7] reported that the  $\text{BaO}-\text{TiO}_2-\text{B}_2\text{O}_3$  glasses with high  $\text{TiO}_2$  contents of 30–40 mol% show large optical basicity of

Table 3

Molar volume  $V_m$ , mean atomic volume  $V_{\text{atom}}$ , calculated packing density  $V_p$ , molar polarizability  $\alpha_m$ , electronic polarizability of oxide ions  $\alpha_{\text{O}^{2-}}$ , and refractive index based optical basicity  $A$  of  $\text{K}_2\text{O-TiO}_2\text{-GeO}_2$  glasses

Sample	$V_m$ (cm <sup>3</sup> /mol) $\pm 0.03$	$V_{\text{atom}}$ (cm <sup>3</sup> /g-atom) $\pm 0.03$	$V_p \pm 0.03$	$\alpha_m$ (Å <sup>3</sup> ) $\pm 0.01$	$\alpha_{\text{O}^{2-}}$ (Å <sup>3</sup> ) $\pm 0.005$	$A \pm 0.003$
50KTG	28.65	9.55	0.574	4.41	2.225	0.919
60KTG	27.87	9.29	0.568	4.32	2.155	0.895
64KTG	27.50	9.17	0.567	4.28	2.129	0.886
60KTG-2	28.97	9.66	0.561	4.27	2.145	0.891
60KTG-3	26.97	8.99	0.568	4.42	2.192	0.908

$A = 0.81\text{--}0.87$  due to the high polarizability of  $\text{TiO}_n$  polyhedra ( $n = 4\text{--}6$ ).

The values of molar volume,  $V_m$ , and mean atomic volume,  $V_{\text{atom}}$ , estimated from the values of density and chemical composition are shown in Table 3. It is seen that both values of  $V_m$  and  $V_{\text{atom}}$  in  $x\text{K}_2\text{O-xTiO}_2\text{-(100-2x)-GeO}_2$  glasses decrease with increasing  $\text{GeO}_2$  content. The ionic radii of  $\text{K}^+$  (eight oxygen coordination number (CN)),  $\text{Ti}^{4+}$  (six CN) and  $\text{Ge}^{4+}$  (four CN) are 0.151, 0.0605, and 0.039 nm, respectively [39]. As the ionic radii of  $\text{O}^{2-}$ , the following values are taken from the consideration of coordination number; 0.142 nm in  $\text{K}_2\text{O}$ , 0.140 nm in  $\text{TiO}_2$  and 0.138 nm in  $\text{GeO}_2$  [39]. We calculated the volume occupied by constituent ions ( $\text{K}^+$ ,  $\text{Ti}^{4+}$ ,  $\text{Ge}^{4+}$ ,  $\text{O}^{2-}$ ) for a given composition by considering their ionic radius and coordination numbers,  $V_{\text{cal}}$ , and for instance, the values of  $V_{\text{cal}} = 16.45 \text{ cm}^3/\text{mol}$  for 50KTG,  $V_{\text{cal}} = 15.84 \text{ cm}^3/\text{mol}$  for 60KTG, and  $V_{\text{cal}} = 15.59 \text{ cm}^3/\text{mol}$  for 64KTG were obtained. In these calculations, the coordination number of  $\text{Ge}^{4+}$  is fixed to four for simplicity. Furthermore, we estimated the packing density,  $V_p$ , of a given composition from the following:

$$V_p = \frac{V_{\text{cal}}}{V_m} \quad (4)$$

The values obtained are given in Table 3, indicating that all glasses have similar values of  $V_p = 0.561\text{--}0.574$ . It is, therefore, considered from the values of  $V_m$ ,  $V_{\text{atom}}$ , and  $V_p$  that there is no drastic change in the glass structure in  $\text{K}_2\text{O-TiO}_2\text{-GeO}_2$  glasses. In  $x\text{K}_2\text{O-xTiO}_2\text{-(100-2x)GeO}_2$  glasses, however, the packing degree of constituent ions decreases very slightly with increasing  $\text{GeO}_2$  content. Hoppe [40] has reported the values of 0.45–0.51 for the packing density of binary  $\text{K}_2\text{O-GeO}_2$  glasses and discussed the coordination number of  $\text{Ge}^{4+}$  ions.

### 3.3. Raman scattering spectra of glasses

The Raman scattering spectra at room temperature for 50KTG, 60KTG, 64KTG, 60KTG-2, and 60KTG-3 glasses are shown in Figs. 2 and 3. Three main broad peaks are observed in all samples, i.e., at around 500, 750–765, and 865  $\text{cm}^{-1}$ . Furthermore, two shoulder peaks are detected at around 580 and 920  $\text{cm}^{-1}$ . As seen in Fig. 2, the relative intensities of the peaks at  $\sim 500$  and

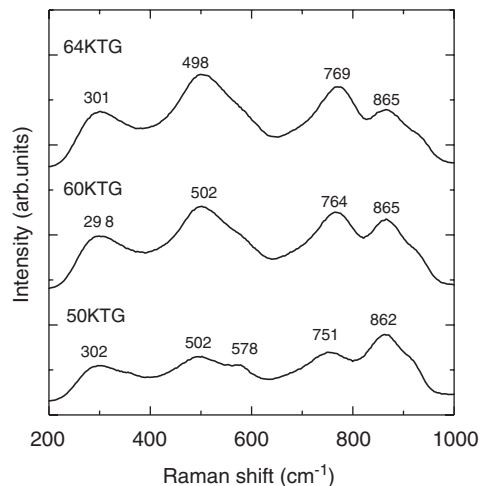


Fig. 2. Raman scattering spectra at room temperature for 50KTG, 60KTG, and 64 KTG glasses. 50KTG:  $25\text{K}_2\text{O-25TiO}_2\text{-50GeO}_2$ , 60KTG:  $20\text{K}_2\text{O-20TiO}_2\text{-60GeO}_2$ , 64 KTG:  $18\text{K}_2\text{O-18TiO}_2\text{-64GeO}_2$ .

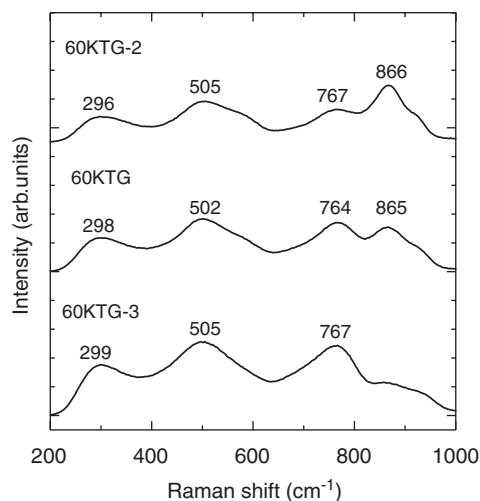


Fig. 3. Raman scattering spectra at room temperature for 60KTG, 60KTG-2, and 60KTG-3 glasses. 60KTG:  $20\text{K}_2\text{O-20TiO}_2\text{-60GeO}_2$ , 60KTG-2:  $25\text{K}_2\text{O-15TiO}_2\text{-60GeO}_2$ , 60 KTG-3:  $15\text{K}_2\text{O-25TiO}_2\text{-60GeO}_2$ .

$750\text{--}765 \text{ cm}^{-1}$  increase with increasing  $\text{GeO}_2$  content, and contrary, the relative intensity of the peak at  $865 \text{ cm}^{-1}$  decreases. For the glasses with a fixed  $\text{GeO}_2$  content of 60 mol% but with different  $\text{K}_2\text{O/TiO}_2$  ratios, the relative



intensity of the peak at  $\sim 765\text{ cm}^{-1}$  decreases largely with increasing  $\text{K}_2\text{O}/\text{TiO}_2$  ratio, and contrary, the relative peak intensity at  $\sim 865\text{ cm}^{-1}$  increases.

So far, many Raman scattering spectra for  $\text{GeO}_2$ -based or  $\text{TiO}_2$ -containing glasses have been reported. For  $\text{GeO}_2$ -based glasses, Raman scattering spectra (i.e., peak position and intensity) relating to vibrations of  $\text{GeO}_4$  tetrahedra change significantly depending on the type and amount of network modifier cations. Basically, however, for  $\text{GeO}_2$ -based glasses, bands in the mid-frequency region of  $\sim 400\text{--}500\text{ cm}^{-1}$  are assigned to symmetric stretching vibrations of  $\text{Ge-O-Ge}$  bonds (bridge) associated with four- and three-membered  $\text{GeO}_4$  rings, and bands in the high-frequency region of  $750\text{--}870\text{ cm}^{-1}$  are assigned to stretching vibrations of  $\text{Ge-O}^-$  bonds (terminal groups) [41–46]. In particular, in alkali germanate glasses, increasing the amount of alkali content results in increasing concentration of non-bridging oxygen (NBO) atoms, and the bands at  $\sim 780$  and  $\sim 870\text{ cm}^{-1}$  have been assigned to symmetric stretching motions of  $\text{Ge-O}^-$  bonds involving two NBO atoms and one NBO atom, respectively. On the other hand, it is also well known that  $\text{TiO}_4$  tetrahedra,  $\text{TiO}_5$  square pyramid and  $\text{TiO}_6$  octahedra in glasses show Raman active bands [47–53]. According to Furukawa and White [47], the frequencies for  $\text{TiO}_4$  are around  $750\text{ cm}^{-1}$ , while those for  $\text{TiO}_6$  are less than  $650\text{ cm}^{-1}$ . When  $\text{TiO}_4$  units are polymerized, the frequencies of the  $\text{Ti-O}$  stretching modes would be expected to increase. On this basis they have assigned the bands at  $910$  and  $880\text{ cm}^{-1}$  in the Raman spectra of  $\text{Li}_2\text{Si}_2\text{O}_6\text{-TiO}_2$  glasses to  $\text{Ti-O}$  stretching vibrations of fourfold coordinated  $\text{Ti}^{4+}$  ions [47]. The previous studies [47–53] suggest the following peak assignments;  $750\text{--}880\text{ cm}^{-1}$  for  $\text{Ti-O}$  stretching vibration of  $\text{TiO}_4$ ,  $\sim 830\text{--}930\text{ cm}^{-1}$  for  $\text{Ti-O}$  stretching vibration of  $\text{TiO}_5$ , and  $\sim 630\text{--}740\text{ cm}^{-1}$  for  $\text{Ti-O}$  stretching vibration of  $\text{TiO}_6$ .

Considering the features of Raman scattering spectra for  $\text{GeO}_2$ -based and  $\text{TiO}_2$ -containing glasses [41–53], the spectra for  $\text{K}_2\text{O-TiO}_2\text{-GeO}_2$  glasses shown in Figs. 2 and 3 are interpreted as follows. (1) The peaks at  $\sim 500\text{ cm}^{-1}$  are assigned to symmetric stretching vibrations of  $\text{Ge-O-Ge}$  bonds in interconnected  $\text{GeO}_4$  tetrahedra. (2) The peaks at  $750\text{--}765\text{ cm}^{-1}$  are assigned to stretching vibrations of  $\text{Ge-O}^-$  bonds with two NBO atoms, and probable coordination polyhedra are  $\text{K}\cdots\text{O-Ge(O}_2\text{)-O}\cdots\text{Ti}$ . Furthermore,  $\text{Ti-O}$  stretching vibrations of  $\text{TiO}_n$  units with  $n$  less than 6 might contribute to these peaks of  $750\text{--}765\text{ cm}^{-1}$ . (3) The peaks at  $\sim 865\text{ cm}^{-1}$  are assigned to stretching vibrations of  $\text{Ge-O}^-$  bonds with one NBO atom, and probable coordination polyhedra are  $\text{Ge(O}_3\text{)-O}\cdots\text{K}$ . (4) The peaks at  $\sim 865\text{ cm}^{-1}$  might include some contributions of  $\text{Ti-O}$  stretching vibrations of  $\text{TiO}_4$  tetrahedra. (5) The two shoulder peaks at  $\sim 580$  and  $920\text{ cm}^{-1}$  might be related to the bending mode of  $\text{Ge-O-Ge}$  bridges involving motion of both O and Ge atoms [45] and to antisymmetric stretching of  $\text{Ge-O-Ge}$  bonds [46], respectively. The structure of  $\text{K}_2\text{O-TiO}_2\text{-GeO}_2$

glasses, in particular the coordination state of  $\text{Ti}^{4+}$  ions will be discussed later.

### 3.4. Crystallization of glasses and second harmonic generation

The XRD patterns at room temperature for the bulk crystallized samples obtained by heat treatment at various temperatures in 60KTG glass ( $T_g = 551\text{ }^\circ\text{C}$ ,  $T_x = 616\text{ }^\circ\text{C}$ ) are shown in Fig. 4. It is seen that the crystallization occurs in the sample heat-treated at  $\sim T_g$  for 3 h. All peaks are assigned to the  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystalline phase [54, JCPDS No.27-394]. It should be pointed out that the chemical composition of 60KTG glass, i.e.,  $20\text{K}_2\text{O-20TiO}_2\text{-60GeO}_2$ , corresponds to the stoichiometric composition of the  $\text{K}_2\text{TiGe}_3\text{O}_9$  phase. The XRD data shown in Fig. 4 indicate that the  $\text{K}_2\text{TiGe}_3\text{O}_9$  phase is formed randomly at the surface of the glass without any orientation. From the XRD analyses for the pulverized samples, it was also confirmed that  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystals are formed in the interior of 60KTG glass, i.e., bulk crystallization. Grujic et al. [32] also reported the formation of  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystals in  $20\text{K}_2\text{O-20TiO}_2\text{-60GeO}_2$  glass. The crystallized samples in 50KTG glass showed XRD patterns similar to the case of 60KTG glass, indicating the random orientation of  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystals at the surface and in the interior of 50KTG glass.

The XRD patterns for the bulk crystallized sample obtained by heat treatment at  $559\text{ }^\circ\text{C}$  for 3 h in 64KTG glass ( $T_g = 554\text{ }^\circ\text{C}$ ,  $T_x = 636\text{ }^\circ\text{C}$ ) are shown in Fig. 5, in which the surface of the bulk sample was polished. The peaks are assigned to the  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystalline phase. It is seen that  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystals are highly oriented at the surface, i.e.,  $c$ -axis orientation. The scanning electron micrograph for the cross-section of this crystallized sample is shown in Fig. 6. The dense formation of crystals with a thickness of  $\sim 2\text{ }\mu\text{m}$  is confirmed, keeping a good optical

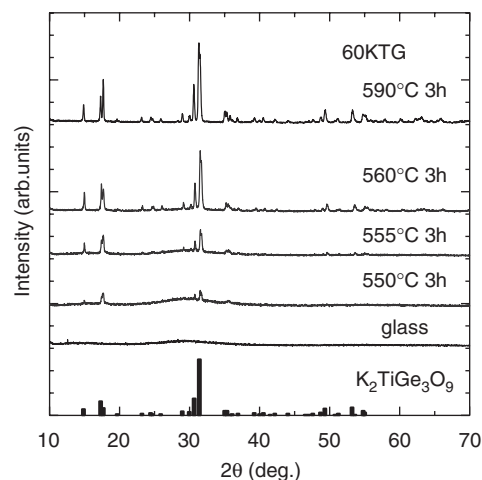


Fig. 4. Powder XRD patterns at room temperature for crystallized samples of 60KTG glass. The peaks are assigned to the  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystalline phase. 60KTG:  $20\text{K}_2\text{O-20TiO}_2\text{-60GeO}_2$ .

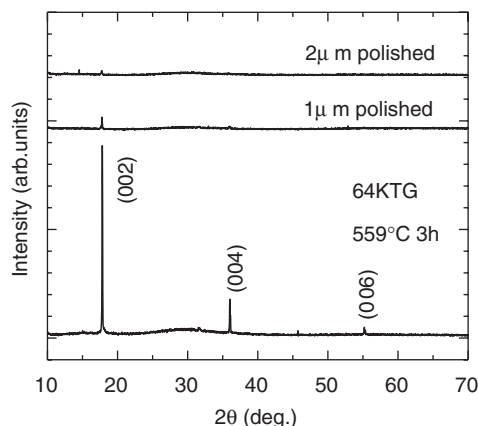


Fig. 5. Bulk XRD patterns at room temperature for crystallized samples of 64KTG glass. The crystalline phase is  $K_2TiGe_3O_9$ . 64KTG:  $18K_2O-18TiO_2-64GeO_2$ .

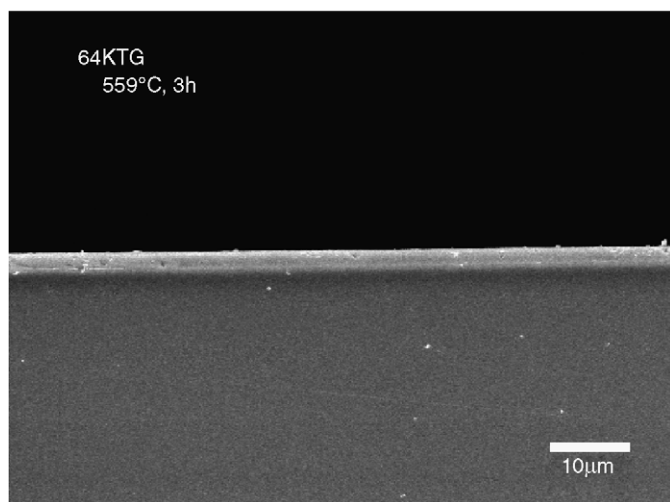


Fig. 6. SEM photograph for the cross-section of the crystallized sample of 64KTG glass. 64KTG:  $18K_2O-18TiO_2-64GeO_2$ .

transparency. In the sample heat-treated at a high temperature of  $636^\circ C$  (crystallization temperature),  $K_2TiGe_3O_9$  crystals are formed randomly in the interior of the glass.

We carried out SHG experiments for crystallized glasses consisting of  $K_2TiGe_3O_9$  crystals. As an example, the Maker fringe pattern for the transparent surface crystallized sample obtained by heat treatment at  $559^\circ C$  for 3 h in 64KTG glass is shown in Fig. 7. The SHG was clearly detected. Furthermore, it is seen that the SH intensity changes depending on the angle of incident light, indicating the orientation of polarized direction at the surface. SHGs were also confirmed in other crystallized samples of 60KTG and 50KTG glasses. No detectable SHGs were observed in the base  $K_2O-TiO_2-GeO_2$  glasses (not crystallized samples) prepared in the present study. That is, the present study suggests that  $K_2TiGe_3O_9$  crystals formed in  $K_2O-TiO_2-GeO_2$  glasses might have some origin for inducing anisotropic polarizations in its structure. The structure of the  $K_2TiGe_3O_9$  phase will be discussed later.

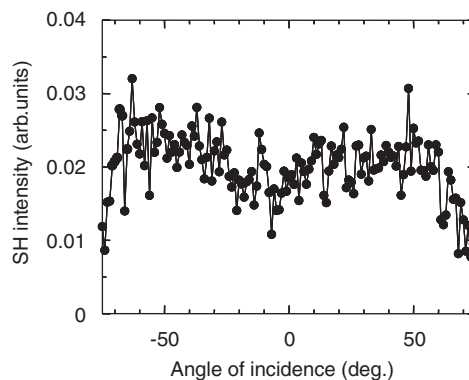


Fig. 7. Maker fringe pattern of SH intensity for the crystallized ( $559^\circ C$ , 3 h) sample of 64KTG glass. 64KTG:  $18K_2O-18TiO_2-64GeO_2$ .

### 3.5. Raman scattering spectra of crystallized glass and the $K_2TiGe_3O_9$ phase

The Raman scattering spectrum at room temperature for  $K_2TiGe_3O_9$  polycrystalline samples prepared by a solid state reaction ( $550^\circ C$ , 10 h +  $840^\circ C$ , 10 h, in air) in the present study are shown in Fig. 8. This is the first report on the Raman scattering spectrum for this crystal. It has been reported that the  $K_2TiGe_3O_9$  phase has a trigonal structure with the lattice constants of  $a = 1.191$  and  $c = 1.001$  nm, space group of  $P\bar{3}c1$  [54,55]. This phase consists of mixed tetrahedral-octahedral framework structures in which three-membered  $[Ge_3O_9]$  rings of  $GeO_4$  tetrahedra are interconnected by isolated  $TiO_6$  octahedra via shared corners. That is, the  $K_2TiGe_3O_9$  phase consists of mixed  $GeO_4$  tetrahedral- $TiO_6$  octahedral framework structures [54,55].

As reported by Graves et al. [56],  $TiO_6$  octahedron gives the following prominent Raman active bands: peaks at  $470-490\text{ cm}^{-1}$  are assigned to torsional modes in  $Ti-O$  bonds, peak at  $\sim 650\text{ cm}^{-1}$  is associated with the symmetric stretching of  $Ti-O$  bonds. It is, therefore, considered that the peaks at  $480$  and  $655\text{ cm}^{-1}$  shown in Fig. 8 are related to  $TiO_6$  octahedra in the  $K_2TiGe_3O_9$  phase. On the other hand, the peaks at  $511$  and  $526\text{ cm}^{-1}$  are assigned to symmetric stretching vibrations of  $Ge-O-Ge$  bonds in interconnected  $GeO_4$  tetrahedra in the  $K_2TiGe_3O_9$  phase [41–46,50]. Furthermore, the peak at  $808\text{ cm}^{-1}$  would be assigned to stretching vibrations of  $Ge-O^-$  bonds with NBO atoms [41–46,50,57]. The peak at  $404\text{ cm}^{-1}$  is probably assigned to bending vibrations of  $GeO_4$  tetrahedra [57].

The Raman scattering spectra for 60KTG glass and crystallized ( $644^\circ C$ , 3 h) sample are shown in Fig. 8. These Raman scattering spectra also indicate that 60KTG glass gives the formation of  $K_2TiGe_3O_9$  crystals through the crystallization. It is noted that both 60KTG glass and crystallized sample have the Raman bands at similar positions, implying structural similarities between the precursor glass and  $K_2TiGe_3O_9$  crystal. That is, it is

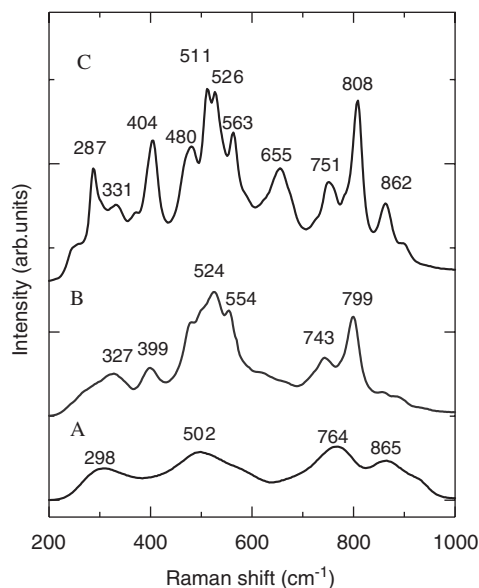


Fig. 8. Raman scattering spectra at room temperature for A: 60KTG glass, B: crystallized (644 °C, 3 h) sample of KTG glass, and C:  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystalline phase prepared by a solid state reaction. 60KTG:  $20\text{K}_2\text{O}-20\text{TiO}_2-60\text{GeO}_2$ .

suggested that  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses examined in this study consist of the network of  $\text{TiO}_6$  and  $\text{GeO}_4$  polyhedra.

The Raman scattering spectrum for  $\text{K}_2\text{TiSi}_3\text{O}_9$  crystals has been reported by Su et al. [52], and a strong peak at  $964\text{cm}^{-1}$  has been assigned to the vibration band of  $\text{Si}(\text{O}_3)-\text{O}\cdots\text{Ti}(\text{O}_5)$  bond. As seen in Fig. 8, there is no peak at around  $950\text{cm}^{-1}$  in the Raman scattering spectrum for  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystals, but the peaks are observed below  $900\text{cm}^{-1}$ . These features indicate that the bond strength of  $\text{Ge}(\text{O}_3)-\text{O}\cdots\text{Ti}(\text{O}_5)$ , i.e., the connection between  $\text{GeO}_4$  and  $\text{TiO}_6$  polyhedra, in  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystals is smaller than that of  $\text{Si}(\text{O}_3)-\text{O}\cdots\text{Ti}(\text{O}_5)$  in  $\text{K}_2\text{TiSi}_3\text{O}_9$  crystals.

As seen in Table 2, 60KTG glass ( $20\text{K}_2\text{O}-20\text{TiO}_2-60\text{GeO}_2$ ) has the values of  $\Delta T = 65^\circ\text{C}$ , where  $\Delta T$  is the difference between crystallization and glass transition temperatures, i.e.,  $\Delta T = T_x - T_g$ , and is known as an indicator for thermal stability against crystallization in glass. On the other hands, 50KTG and 64KTG glasses have the values of  $\Delta T = 81$  and  $82^\circ\text{C}$ , respectively. These results suggest that 60KTG glass with the composition corresponding to the stoichiometric  $\text{K}_2\text{TiGe}_3\text{O}_9$  has a relatively low thermal stability against crystallization in  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses. This might also support the structural similarity between 60KTG glass and  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystal.

#### 4. Discussion

One of the main purposes of this study was to explore new transparent crystallized glasses showing SHGs in the ternary  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses with high  $\text{TiO}_2$  contents of 15–25 mol%. In the glasses examined in the present study, the crystalline phase formed through crystallization

is  $\text{K}_2\text{TiGe}_3\text{O}_9$ . It should be pointed out that there is an inversion symmetry for the trigonal structure with a space group of  $P\bar{3}c1$ , meaning that in principle, the  $\text{K}_2\text{TiGe}_3\text{O}_9$  phase would not show any second-order optical nonlinearities. But, SHGs were observed in the crystallized samples consisting of  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystals.

The structural unit of  $\text{TiO}_6$  octahedron in the  $\text{K}_2\text{TiGe}_3\text{O}_9$  phase is shown in Fig. 9. It is seen that the  $\text{TiO}_6$  octahedron is not symmetrical, but is largely distorted. A ferroelectric origin in  $\text{BaTi}_2\text{O}_5$  crystal has been proposed to be due to the distortion of  $\text{TiO}_6$  octahedra [58,59]. It should be pointed out that at first the  $\text{BaTi}_2\text{O}_5$  phase had been reported to have a centrosymmetric structure [60]. It is well known that a large second-order optical nonlinearity in transparent crystallized glasses consisting of fersnoite-type  $\text{Ba}_2\text{TiGe}_2\text{O}_8$  crystals is induced by the presence of  $\text{TiO}_5$  pyramidal units in the crystal structure [15,16,61]. Considering the relation between second-order optical nonlinearity/ferroelectricity and distortion of  $\text{TiO}_n$  polyhedra in  $\text{TiO}_2$ -based crystals [15,16,58–61], it would be reasonable to conclude that SHGs in the crystallized samples of  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses come from the distortion in  $\text{TiO}_6$  octahedra in  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystals. Furthermore, it is considered that  $\text{TiO}_6$  octahedra in  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses might be distorted, consequently giving a strong effect on the electronic polarizability of the glasses.

The electronic polarizability of oxide ions and optical basicity in  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses increase with increasing  $\text{K}_2\text{O}$  and  $\text{TiO}_2$  or with decrease of  $\text{GeO}_2$  content. As reported by Dimitrov and Sakka [30], the simple oxides  $\text{TiO}_2$  and  $\text{GeO}_2$  have the following values:  $\alpha_{\text{O}^{2-}} = 2.368\text{Å}^3$  and  $A = 0.96$  for  $\text{TiO}_2$  (rutile) and  $\alpha_{\text{O}^{2-}} = 1.720\text{Å}^3$  and  $A = 0.70$  for  $\text{GeO}_2$ . According to Duffy [62], optical basicity of  $\text{K}_2\text{O}$  is 1.4. That is the degree of basicity (electron donor ability of oxide ions) in simple oxides of  $\text{K}_2\text{O}$ ,  $\text{TiO}_2$ , and  $\text{GeO}_2$  is in the order:  $\text{GeO}_2 < \text{TiO}_2 < \text{K}_2\text{O}$ . The general trend that the electronic polarizability of oxide ions in  $\text{K}_2\text{O}-\text{TiO}_2-\text{GeO}_2$  glasses increases with the

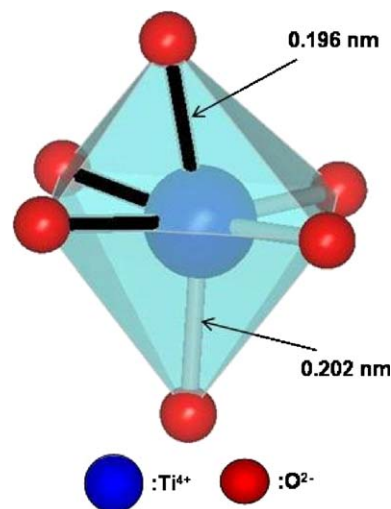


Fig. 9.  $\text{TiO}_6$  octahedron in the  $\text{K}_2\text{TiGe}_3\text{O}_9$  crystalline phase.



substitution of  $K_2O$  and  $TiO_2$  for  $GeO_2$  seems, therefore, to be reasonable. For example,  $25K_2O-25TiO_2-50GeO_2$  glass possesses the highest values of  $\alpha_{O^{2-}} = 2.25 \text{ \AA}^3$  and  $A = 0.919$ . Dimitrov and Komatsu [63,64] applied the interaction parameter  $A$  proposed by Yamashita and Kurosawa [65] to describe the polarizability state of an average oxide ion in numerous simple oxides and binary oxide glasses and its ability to form an ionic-covalent bond with a cation. The interaction parameter is a quantitative measure for the interionic interaction of negative ions such as  $O^{2-}$  with the nearest neighbors (cations). They proposed the following values:  $A = 0.081 \text{ \AA}^{-3}$  for  $TiO_2$  and  $A = 0.146 \text{ \AA}^{-3}$  for  $GeO_2$  [63,64]. The increase in polarizability of the oxide ion as well as optical basicity of simple oxides or oxide glasses could be explained with decreased interaction inside the ionic pair, resulting in a smaller overlap between oxygen  $2p$  and cation valence orbitals to form a chemical bond [63,64]. That is, the concept of interaction parameter suggest that Ti–O bonds are more ionic compared with Ge–O bonds. Considering the above, it is expected that the optical nonlinearity of  $K_2O-TiO_2-GeO_2$  glasses with high  $TiO_2$  contents is in close relation with the presence in the structure of  $TiO_n$  ( $n = 4-6$ ) units with high polarizability.

Laudisio et al. [66] studied the devitrification behavior of  $Li_2O-TiO_2-GeO_2$  glasses such as  $20Li_2O-20TiO_2-60GeO_2$  (i.e.,  $Li_2TiGe_3O_9$ ), but the crystalline phases formed in the glasses with high  $TiO_2$  contents have not been identified. To our knowledge, there has been no report on the synthesis (presence) of  $Li_2TiGe_3O_9$  crystalline phase. As indicated in the present study,  $K_2TiGe_3O_9$  crystals are formed easily through the crystallization of  $K_2O-TiO_2-GeO_2$  glasses with high  $TiO_2$  contents. In particular, as shown in Figs. 1 and 4, the glass with the composition corresponding to the stoichiometric  $K_2TiGe_3O_9$  shows a prominent crystallization of  $K_2TiGe_3O_9$ .

Muller et al. [67] proposed that in the structure of various  $SiO_2$ -based glasses showing homogeneous nucleation both cationic and anionic arrangements in glass and crystal are similar. Although the microstructure of the crystallized glasses of  $20K_2O-20TiO_2-60GeO_2$  has not been examined, the data shown in Figs. 1 and 4 suggest that the homogeneous nucleation occurs in this glass. It has been reported that the glass of  $40BaO-20TiO_2-40SiO_2$  (i.e.,  $Ba_2TiSi_2O_8$ ) shows extremely high nucleation rates, giving nanocrystallized glasses consisting of nonlinear optical  $Ba_2TiSi_2O_8$  nanocrystals [9,10,68]. Very recently, Gupta et al. [22] succeeded in developing transparent nanocrystallized glasses consisting of  $LaBGeO_5$  nanocrystals through a two-step heat treatment in  $25La_2O_3-25B_2O_3-50GeO_2$  (i.e.,  $LaBGeO_5$ ) glass. Furthermore, our research group [25,26] found that the glass of  $25K_2O-25Nb_2O_5-50GeO_2$  shows a prominent nanocrystallization, in which the glass composition is close to that of  $K_{3.8}Nb_5Ge_3O_{20.4}$  nanocrystals formed in that glass. Considering these previous studies, even in  $K_2O-TiO_2-GeO_2$  glasses, we believe that some glasses, e.g., close to  $20K_2O-20TiO_2-60GeO_2$ , might show

nanocrystallization through careful heat treatment and small modification of glass composition, and such a study is now under consideration.

## 5. Conclusions

$K_2O-TiO_2-GeO_2$  glasses with a large amount of  $TiO_2$  contents (15–25 mol%) such as  $25K_2O-25TiO_2-50GeO_2$  were prepared to search new nonlinear optical crystallized glasses showing second harmonic generations (SHGs). It was proposed from Raman scattering spectra that the glasses consist of the network of  $TiO_6$  and  $GeO_4$  polyhedra. The glasses showed large optical basicities of  $A = 0.88-0.92$ , indicating the high polarizability of  $TiO_6$  and  $GeO_4$  polyhedra in the glasses. It was found from XRD analyses and Raman scattering spectra that  $K_2TiGe_3O_9$  crystals were formed through crystallization. In particular, the surface crystallization giving the  $c$ -axis orientation of  $K_2TiGe_3O_9$  crystals was found in  $18K_2O-18TiO_2-64GeO_2$  glass. The crystallized glasses showed SHGs, and it was suggested that the distortion of  $TiO_6$  octahedra in  $K_2TiGe_3O_9$  crystals induces SHGs.

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